

# Spectra, Thresholds, and Modal Fields of a Triangular Microcavity Laser

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## Abstract

© 2018 IEEE. We study the modes of a triangular microcavity laser, namely the frequencies of emission, threshold values of gain, and mode field patterns, within the classical electromagnetics approach. Our instrument is the accurate formalism of Lasing Eigenvalue Problem (LEP), i.e. boundary-value problem with full set of the boundary and radiation conditions. The LEP is reduced to a nonlinear eigenvalue problem for the Muller integral equation on the cavity's boundary. Discretizing it with a Nyström approximation of weakly singular integral operators, we obtain a characteristic equation for the mode frequencies and thresholds.

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## Keywords

lasing eigenvalue problem, microcavity laser, Muller boundary integral equation, Nyström method

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